



**UNIVERSITY OF MINES AND TECHNOLOGY, TARKWA**  
**SECOND SEMESTER EXAMINATIONS, MAY 2018**

COURSE NO: MR 358  
 COURSE NAME: **HEAT TRANSFER**  
 CLASS: BSc MR III/MC III

TIME: 3 HRS

Name: \_\_\_\_\_ Index Number: \_\_\_\_\_

**ATTEMPT ANY THREE QUESTIONS**

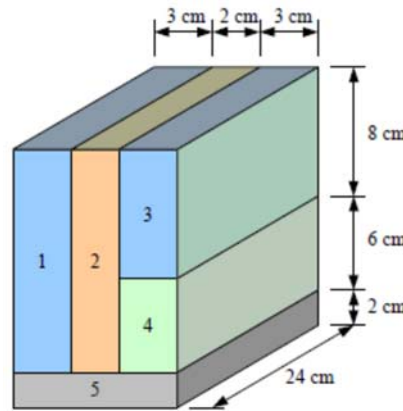
**Q1.** a) Explain, define or state each of the following heat transfer terms/laws:

- i) Conduction                      ii) Convection                      iii) Radiation
- iv) Blackbody    v) Gray body

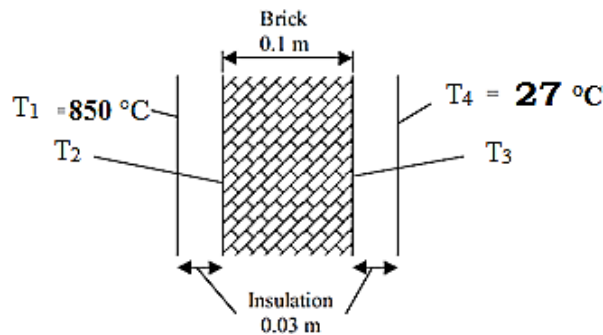
**[10 marks]**

b) A composite panel consists of five sections, as shown in the figure.  $k_1 = k_3 = 160 \text{ W/m.K}$ ;  $k_2 = 220 \text{ W/m.K}$ ;  $k_4 = 200 \text{ W/m.K}$ , and  $k_5 = 270 \text{ W/m.K}$ .

- i) Construct the thermal circuit model and find the total thermal resistance. **[15 marks]**
- ii) If  $T_{\text{left}} = 25 \text{ }^\circ\text{C}$ ,  $T_{\text{right}} = 180 \text{ }^\circ\text{C}$  and  $h = 25 \text{ W/m}^2\text{.K}$  on both sides, find the heat transfer rate through the composite. **[8 marks]**



**Q2.** Consider the heat transfer situation illustrated below:

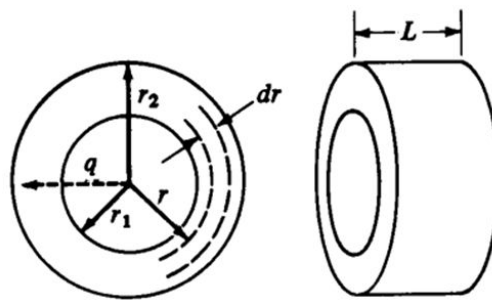


- a) Represent this system by a suitable circuit diagram of resistances **[5 marks]**
- b) Determine the individual and overall thermal resistances across the system per unit area **[16 marks]**
- c) Calculate the overall heat flux  $q$  across the insulating wall in  $\text{W/m}^2$  **[4 marks]**
- d) Estimate the temperatures  $T_2$  and  $T_3$  in  $^\circ\text{C}$ . **[8 marks]**

Assume  $k_{\text{brick}} = k_2 = 0.72 \text{ W/m-K}$ ;

$k_{\text{insulation}} = k_1 = k_3 = 0.067 \text{ W/m-K}$

**Q3.** a) Use Fourier's law to derive an expression for the heat flow  $q$ , through the concentric cylinder illustrated below: **[6 marks]**



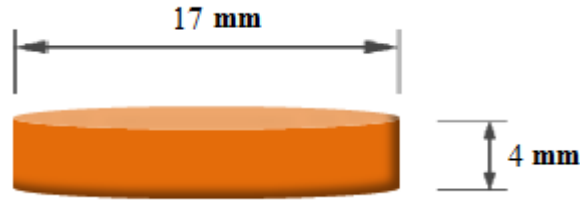
b) A cylindrical tube 120 mm OD is insulated with a 60-mm layer of silica foam, for which the conductivity is  $0.0625 \text{ W/m-}^\circ\text{C}$ , followed with a 36-mm layer of cork with a conductivity of  $0.0525 \text{ W/m-}^\circ\text{C}$ . If the temperature of the outer surface of the pipe is  $250 \text{ }^\circ\text{C}$  and the temperature of the outer surface of the cork is  $30 \text{ }^\circ\text{C}$ , calculate:

- i) The logarithmic mean radius for the silica layer **[5 marks]**
- ii) The logarithmic mean radius for the cork layer **[5 marks]**
- iii) The heat loss in watts per meter of pipe. **[5 marks]**

c) A sudden cold wave drops the atmospheric temperature of an environment from  $6 \text{ }^\circ\text{C}$  to  $-32 \text{ }^\circ\text{C}$  for 18h. The thermal diffusivity of soil is  $0.0011 \text{ m}^2/\text{h}$

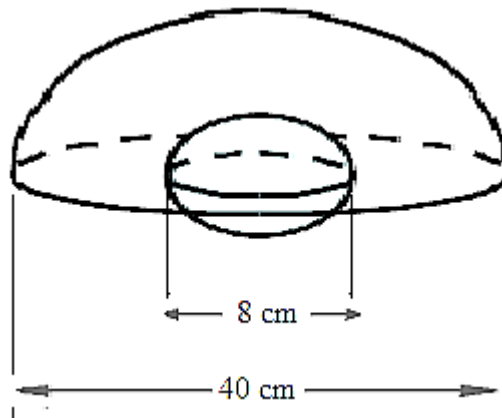
- i) How deep would a water pipeline have to be buried to be in no danger of freezing? **[6 marks]**
- ii) What is the penetration distance under these conditions? **[6 marks]**

**Q4** a) A hot cylindrical pellet of hausmannite ( $\text{Mn}_3\text{O}_4$ ) of 17 mm diameter and 4-mm thickness having a surface temperature of  $1150 \text{ }^\circ\text{C}$  is suddenly exposed to an environment of temperature  $27 \text{ }^\circ\text{C}$ .



The convective heat transfer coefficient can be approximated as  $45 \text{ W/m}^2\cdot\text{K}$  on the top and the side surfaces, and  $25 \text{ W/m}^2\cdot\text{K}$  on the bottom surface and the emissivity of the cylindrical  $\text{MnO}$ -pellet is  $0.68$  on all sides. Neglecting the effects of heat loss due to conduction, calculate the rate of heat loss from the pellet to the air. **[16 marks]**

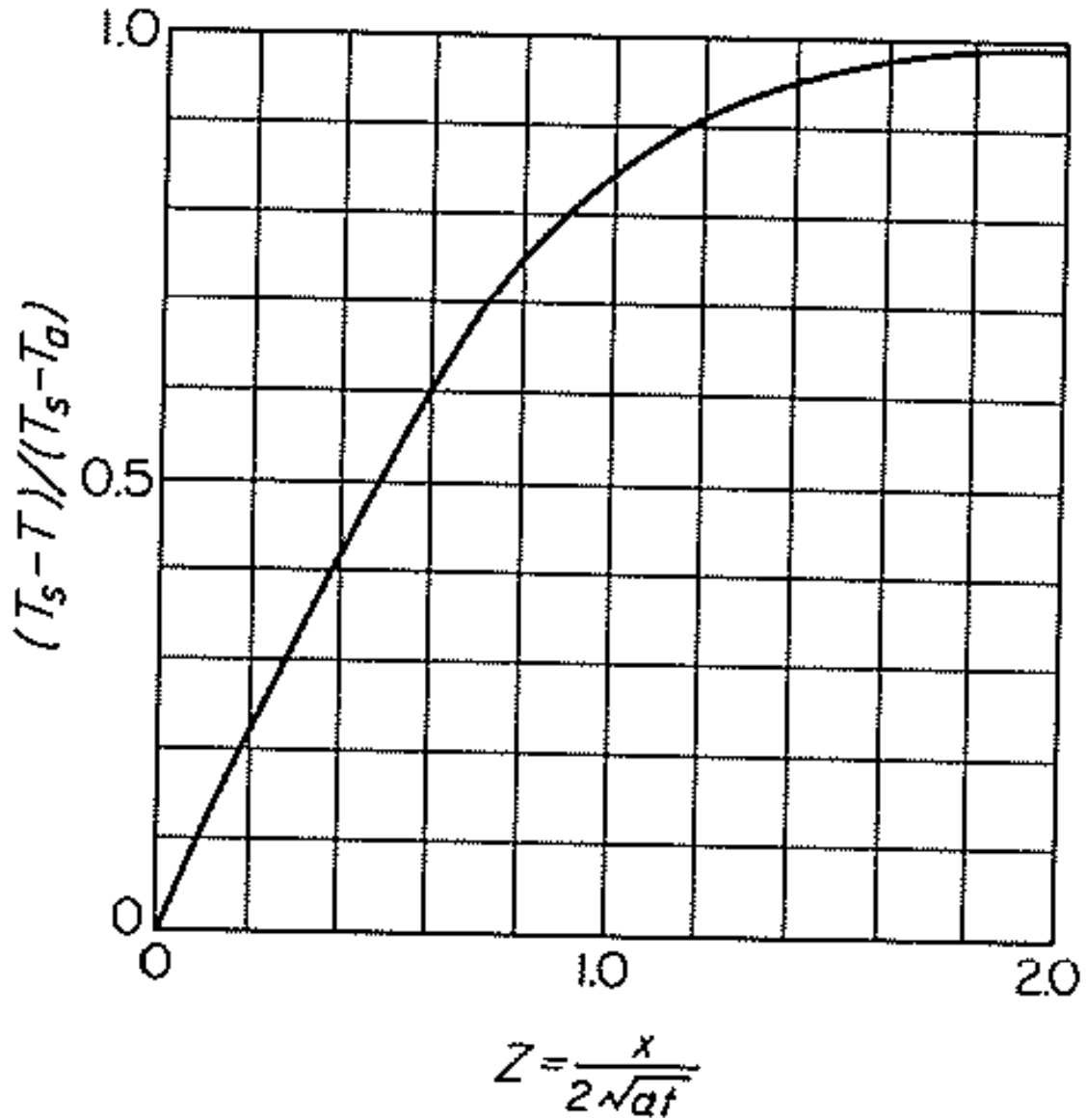
b) A  $40 \text{ cm}$  diameter dome at  $450 \text{ }^\circ\text{C}$ , with absorptivity and emissivity of  $1$  is placed over an  $8 \text{ cm}$  diameter glass sphere at  $250 \text{ }^\circ\text{C}$  and suspended in the air so that the dome and sphere are concentric. The properties of the glass sphere are:  $k = 1.4 \text{ W/m}\cdot\text{K}$ ,  $\rho = 2225 \text{ kg/m}^3$ ,  $c_p = 835 \text{ J/kg}\cdot\text{K}$ ,  $\varepsilon = 0.9$ ,  $\alpha = 0.8$



Find:

- i) The rate of heat loss due to convection from the sphere if convection coefficient is  $15 \text{ W/m}^2\cdot\text{K}$  and the air temperature is  $20 \text{ }^\circ\text{C}$ . **[2 ½ marks]**
- ii) The rate of heat loss from the sphere due to radiation. **[2 ½ marks]**
- iii) The shape factor from the sphere to the dome. **[2 ½ marks]**
- iv) The shape factor from the dome to the sphere. **[2 ½ marks]**
- v) The rate of heat loss from the inside surface of the dome. **[2 ½ marks]**
- vi) The rate of heat transfer from the inside surface of the dome to the sphere. **[2 ½ marks]**
- vii) The net heat transfer of the sphere. Is the sphere losing heat or gaining heat? **[2 marks]**

*Course Examiners: J. R. Dankwah/*



$$\frac{T_s - T}{T_s - T_a} = \frac{2}{\sqrt{\pi}} \int_0^Z e^{-Z^2} dZ$$

$$Z = \frac{x}{2\sqrt{\alpha t}}$$