

**UNIVERSITY OF MINES AND TECHNOLOGY**  
**DEPARTMENT OF MATHEMATICAL SCIENCES**

MA 379 Element of Topology

Date: February 16, 2021

Quiz1

Time: 45 min

- 1) Define the term topology. Consider the following topology on  $X=\{a,b,c,d,e\}$ ,  
 $\tau=\{X,\emptyset,\{a\},\{a,b\},\{a,c,d\},\{a,b,c,d\},\{a,b,e\}\}$
- I. List the closed subset of  $X$
  - II. Determine the closure of the set  $\{a\},\{b\}$  and  $\{e,c\}$ .
  - III. Which set in (ii) are dense in  $X$ ?

- 2) Define a metric space. Check whether or not

$$\rho(x,y)=\sum_{i=1}^{\infty} \frac{1}{2^i} \frac{|x_i-y_i|}{1+|x_i-y_i|} \quad \forall x,y \in X \text{ is a metric on } X.$$

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